

Discovering a motif discovering approach

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Contents

Goal of the exercise	1
Create a workspace for this practical	1
Loading the data table	1
Exploring observed and expected counts	2
Computing over-representation significance	5

Goal of the exercise

The goal of this exercise is to get an intuition of a motif discovery approach relying on the detection of over-represented oligonucleotides.

Our approach will be pragmatic.

We retrieved the upstream non-coding sequences of the genes involved in methionine biosynthesis and sulfur assimilation, and counted the occurrences of each hexanucleotide.

We also computed

- the relative frequencies (occurrences of each oligo / sum of all oligo occurrences) in the sequence of interest (the promoters of methionine-associated genes)
- the relative frequencies of each hexanucleotide in the whole set of yeast promoters.

We would like to know if some 6nt are over-represented in promoters of methionine-associated genes relative to the occurrences that would be expected from a random selection of yeast promoters.

Create a workspace for this practical

- In your home directory, create a work directory for this practical (for example ~/LCG_BEII/practical_motif_discovery/)

```
workdir <- "~/LCG_BEII/practical_motif_discovery"
dir.create(workdir, showWarnings = FALSE, recursive = TRUE)
setwd(workdir)
```

Loading the data table

1. Download the oligonucleotide count table. Scerevisiae_MET-genes_oligos-6nt-2str-noov_occ-freq.tsv

```
oligo.url <- "http://jvanheld.github.io/LCG_BEII/practicals/motif_discovery/data/Scerevisiae_MET-genes_oligos-6nt-2str-noov_occ-freq.tsv"
oligo.file <- basename(oligo.url) ## Suppress the URL path and keep only the file name for local storage
download.file(oligo.url, destfile = oligo.file)
```

2. In **R**, open a new script or R markdown file.
3. Load the data table, print the 5 top rows and the 5 bottom rows.

```
oligo.table <- read.delim(oligo.file, header = 1, row.names = 1)
# View(oligo.table)
```

```
head(oligo.table, n = 5)
```

	obs_freq	exp_freq	occ	exp_occ
aaaaaa tttttt	0.004592808	0.004896299	41	43.71
aaaaac gttttt	0.001120197	0.001998518	10	17.84
aaaaag cttttt	0.003696651	0.003604251	33	32.18
aaaaat attttt	0.004032710	0.004160627	36	37.14
aaaaca tgtttt	0.001344237	0.001932479	12	17.25

```
tail(oligo.table, n = 5)
```

	obs_freq	exp_freq	occ	exp_occ
ttccaa ttggaa	0.0008961577	0.0008428396	8	7.52
ttcgaa ttcgaa	0.0001120197	0.0003224542	1	2.88
ttgaaa tttcaa	0.0019043352	0.0019087053	17	17.04
ttgcaa ttgcaa	0.0001120197	0.0004030214	1	3.60
tttaaa tttaaa	0.0005600986	0.0009379354	5	8.37

Exploring observed and expected counts

4. Draw an histogram of the observed occurrences and evaluate the spread of counts.

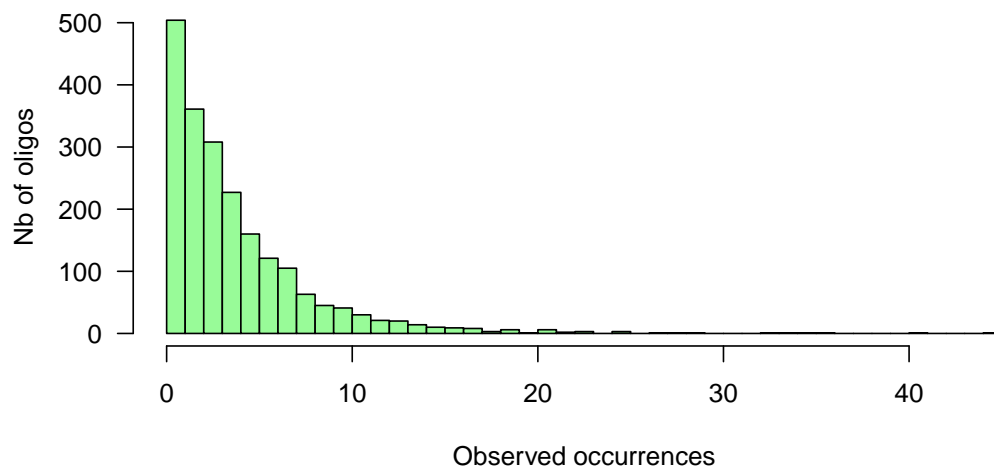
```
x <- oligo.table$occ  
range(x)
```

```
[1] 0 45
```

```
max.x <- max(x)
```

```
hist(x, breaks = 0:max.x, col = "palegreen",  
     xlab = "Observed occurrences",  
     ylab = "Nb of oligos",  
     las = 1,  
     main = "Distribution of oligonucleotide occurrences")
```

Distribution of oligonucleotide occurrences



5. Draw a scatter plot comparing the observed and expected occurrences for each hexanucleotide.

Observed vs expected occurrences

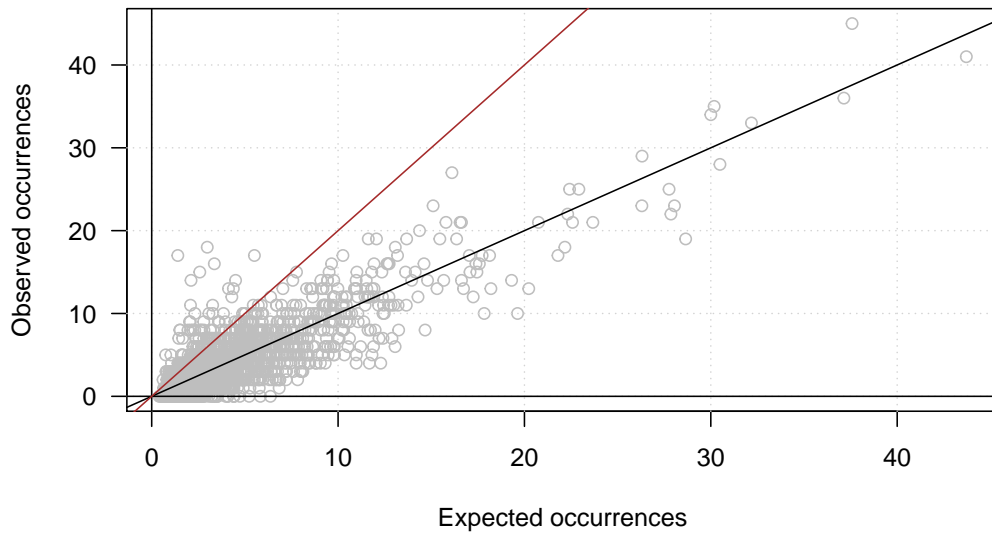


Figure 1: ****Scatter plot of observed versus expected occurrences.**** The black diagonal corresponds to the null hypothesis, the brown line denotes an arbitrary threshold on fold-change > 2 .

```
exp.occ <- oligo.table$exp_occ

plot(exp.occ, x, col = "grey", las = 1,
     xlab = "Expected occurrences",
     ylab = "Observed occurrences",
     main = "Observed vs expected occurrences")
grid()
abline(a = 0, b = 1, col = "black")
abline(h = 0, col = "black")
abline(v = 0, col = "black")

abline(a = 0, b = 2, col = "brown")
```

6. Compute the ratio of observed / expected occurrences, and draw a scatter plot with this ratio (Y) as a function of the expected occurrences (X).

```
ratio <- (x/exp.occ)

plot(exp.occ, ratio,
     col = "grey", las = 1,
     xlab = "Expected occurrences",
     ylab = "(obs/exp) ratio",
     main = "(obs/exp) ratio")
grid()
abline(h = 1, col = "black")
abline(h = 2, col = "brown")
```

6. Compute the log-ratio of observed / expected occurrences, and draw a scatter plot with this log-ratio (Y) as a function of the expected occurrences (X).

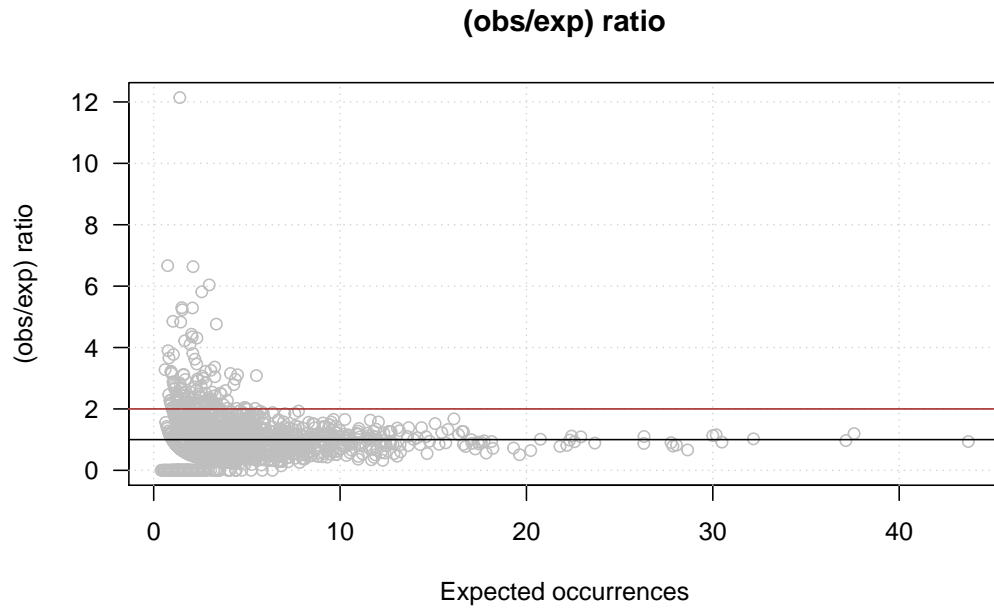


Figure 2: **Scatter plot of observed versus expected occurrences.** The black diagonal corresponds to the null hypothesis, the brown line denotes an arbitrary threshold on fold-change > 2 .

```
lr <- log(x/exp.occ)
oligo.table$lr <- lr

plot(exp.occ, lr,
     col = "grey", las = 1,
     xlab = "Expected occurrences",
     ylab = "log(obs/exp)",
     main = "Log-ratio")
grid()
abline(h = 0, col = "black")
abline(h = log(2), col = "brown")
```

$$lr = \log(x / \langle X \rangle)$$

7. Compute the log-likelihood ratio (llr), defined below, and draw a scatter plot with this llr as a function of the expected occurrences.

$$llr = f \cdot \log(x / \langle X \rangle)$$

```
p <- oligo.table$exp_freq
llr <- p * log(x/exp.occ)
oligo.table$llr <- llr

plot(exp.occ, llr,
     col = "grey", las = 1,
     xlab = "Expected occurrences",
     ylab = "llr",
     main = "Log-likelihood ratio")
grid()
```

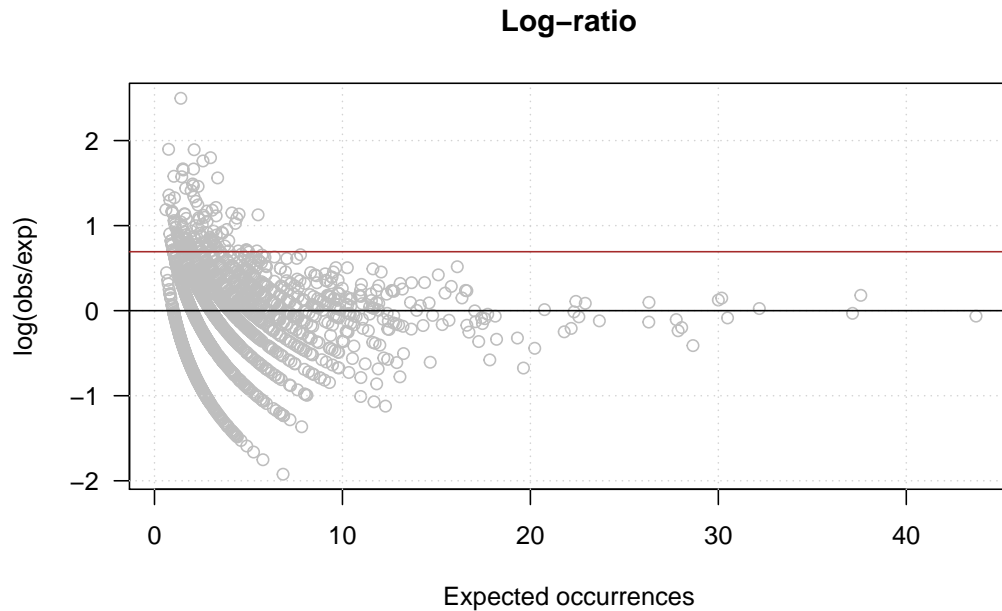


Figure 3: **Scatter plot of observed versus expected occurrences.** The black diagonal corresponds to the null hypothesis, the brown line denotes an arbitrary threshold on fold-change > 2 .

```
abline(h = 0, col = "black")
# abline(h = log(2), col = "brown")
```

Computing over-representation significance

8. Draw a binomial distribution with parameters $n = 8000$, $p = 0.0001$.

```
n <- 8000
p <- 0.001
x <- 15# Number of successes
X <- 0:40 ## values to display

plot(X, dbinom(x = X, size = n, prob = p), type = "h", col = "grey",
      ylab = "P(X = x)", las = 1,
      xlab = "X (nb of successes)")
arrows(x, 0.04, x, 0.02, lwd = 2, length = 0.1, angle = 30, col = "red")

tail <- x:40
lines(tail, dbinom(x = tail, size = n, prob = p), type = "h", col = "red")
arrows(x, 0.04, x, 0.02, lwd = 2, length = 0.1, angle = 30, col = "red")

pval <- pbinom(q = x - 1, size = n, prob = p, lower.tail = FALSE)
legend("topright", legend = paste("pval =", signif(digits = 3, pval)))
```

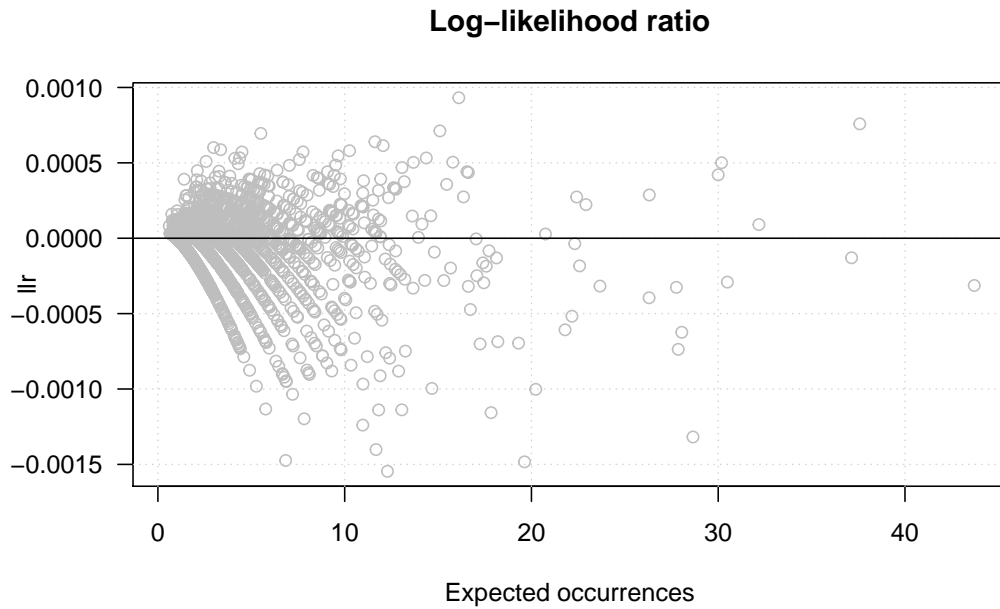
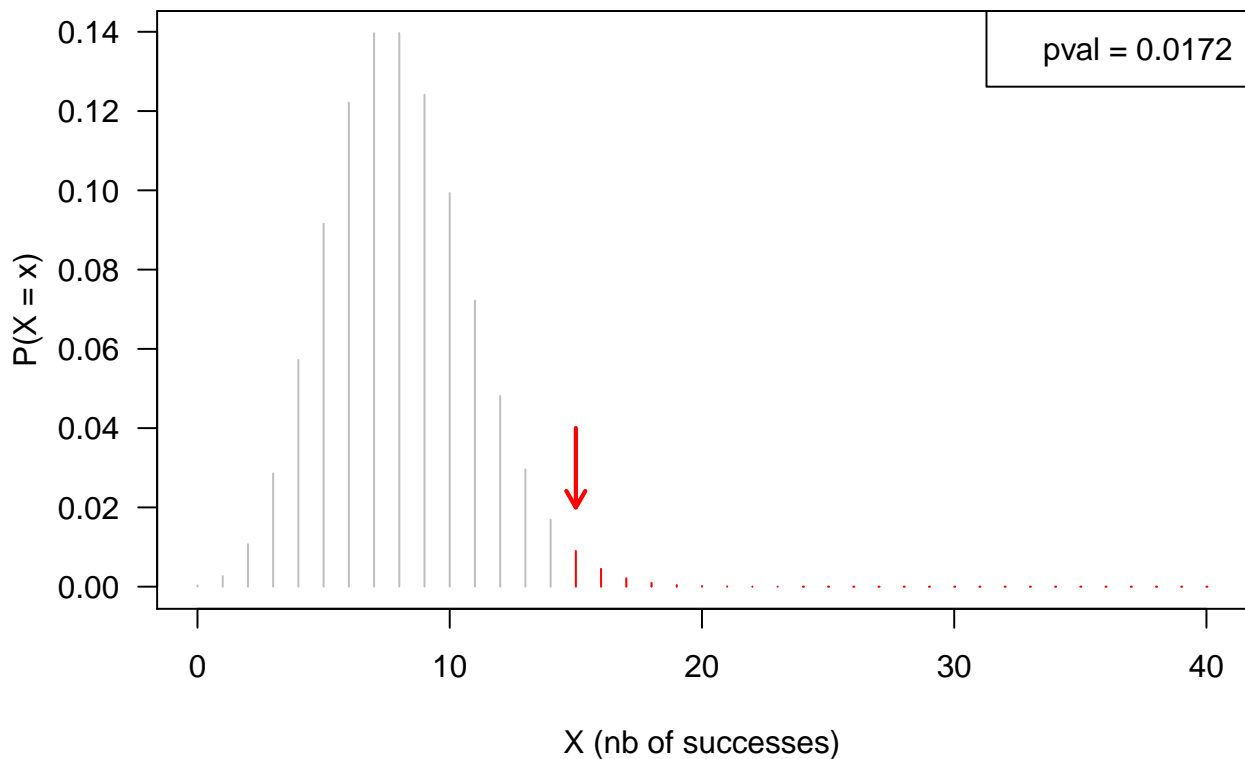


Figure 4: **Scatter plot of log-likelihood ratio (llr) versus expected occurrences.** The black line corresponds to the null hypothesis, the brown line denotes an arbitrary threshold on fold-change > 2.



8. Use the binomial distribution to compute the P-value of the observed occurrences.

$$P = T(X \geq x)$$

```
x <- oligo.table$occ ## Number of successes
n <- sum(x) ## Number of trials
```

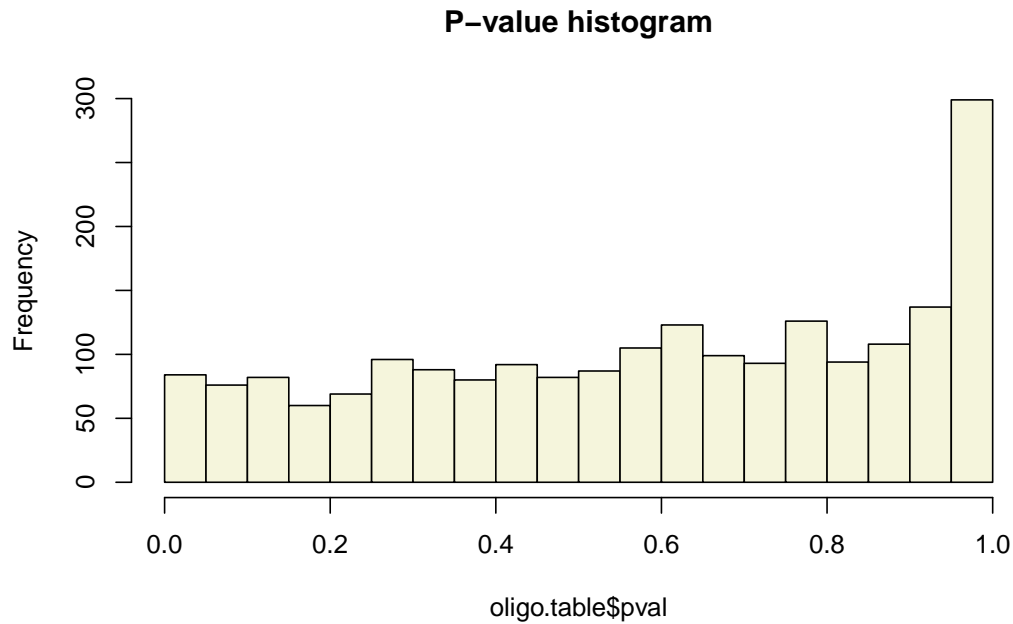


Figure 5: **Histogram of nominal p-values** for all the hexanucleotides grouped by pairs of reverse complements.

```
p <- oligo.table$exp_freq ## Success probability

p <- p / sum(p) # A correction for the fact that we discarded self-overlapping occurrences
# sum(p)

nbTests <- length(x) # Number of tests

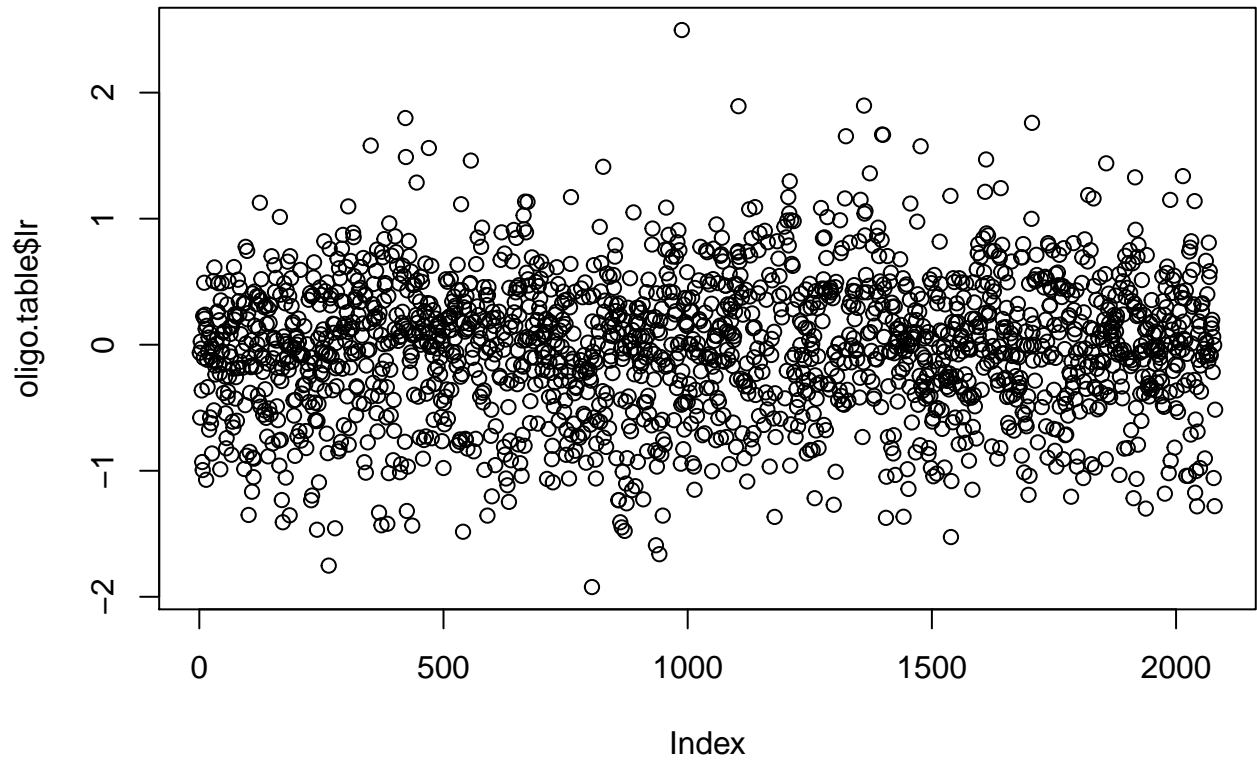
## Compute a P-value for each individual oligonucleotide
oligo.table$pval <- pbinom(q = x - 1, size = n, prob = p, lower.tail = FALSE)
```

9. Draw an histogram with the P-values of all hexanucleotides, with 20 bins.

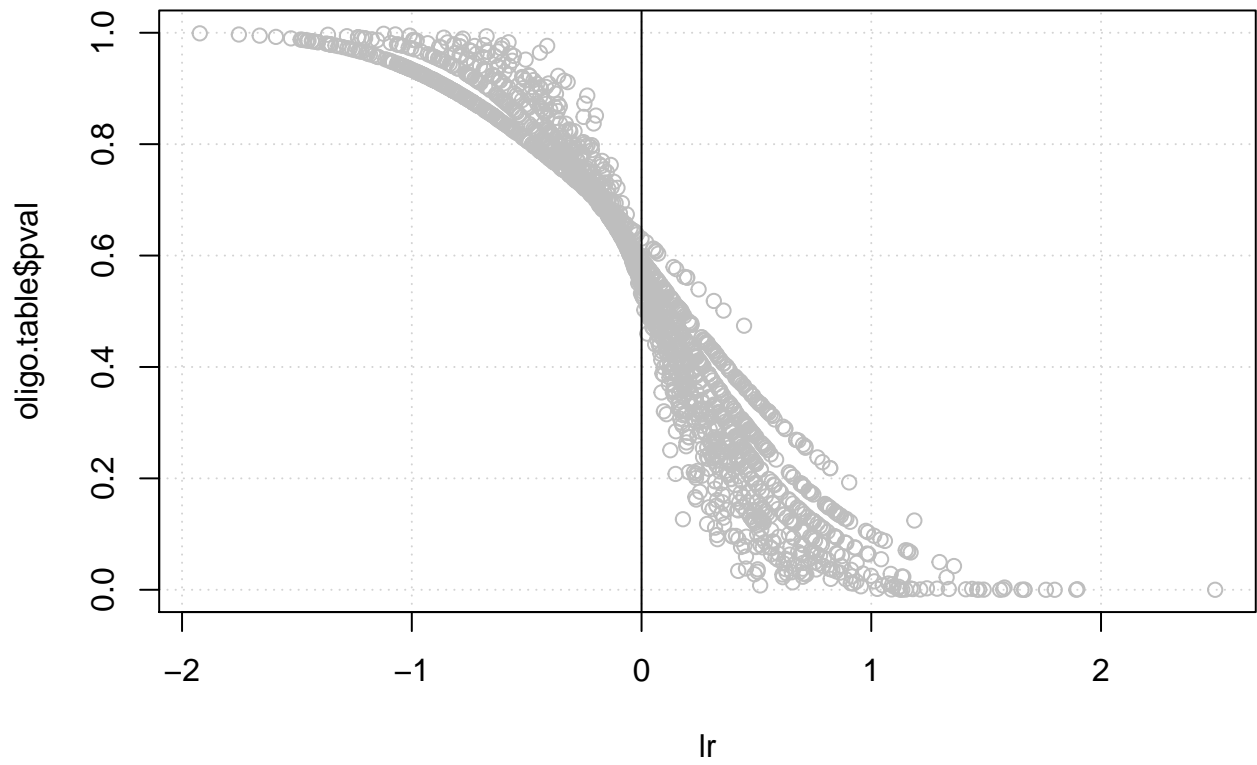
```
hist(oligo.table$pval, breaks = seq(0, 1, 0.05),
     col = "beige", main = "P-value histogram")
```

10. Draw a scatter plot with the P-value (Y) as a function of the log-ratio (X).

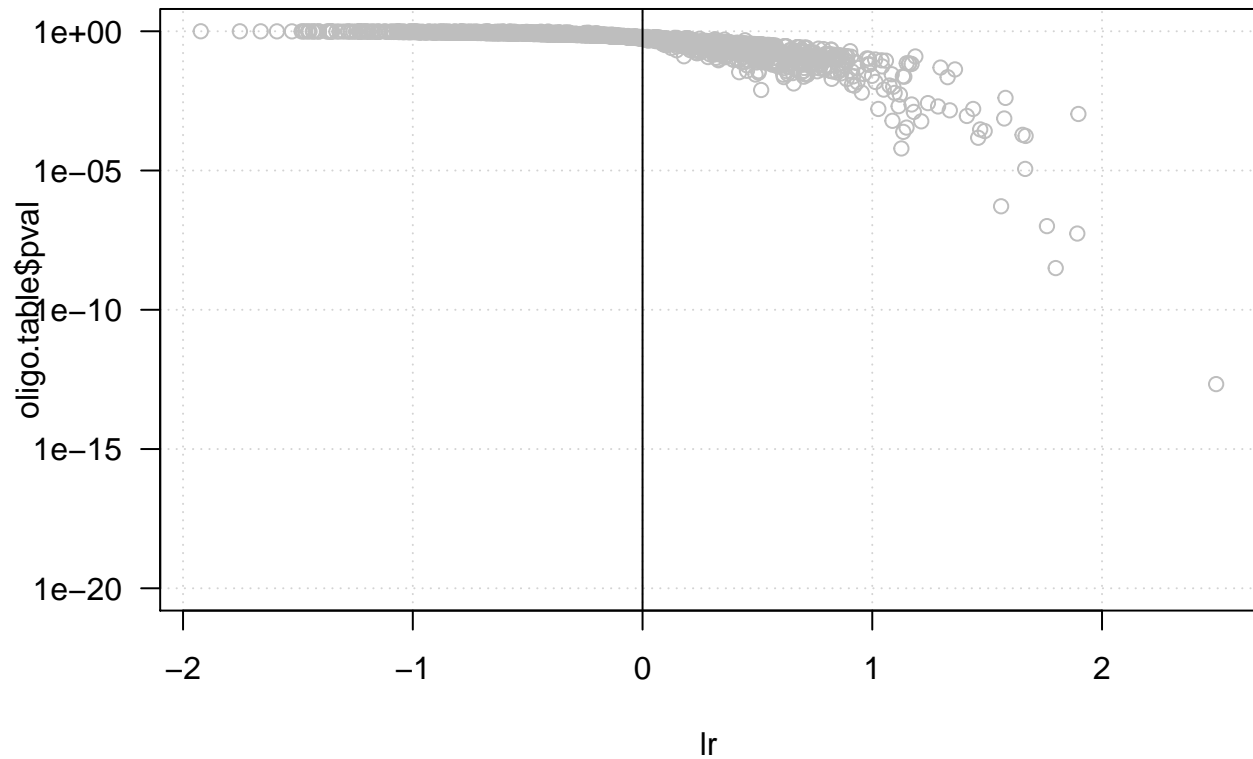
```
plot(oligo.table$lr)
```



```
# hist(lr, breaks = 50)  
plot(lr, oligo.table$pval, col = "grey", panel.first = grid())  
abline(v = 0)
```




```
# hist(lr, breaks = 50)
plot(lr, oligo.table$pval, col = "grey",
     log = "y", las = 1, ylim = c(1e-20, 1),
     panel.first = grid())
abline(v = 0)
```



11. Compute the E-value, and the significance.

$$E = P \cdot N$$

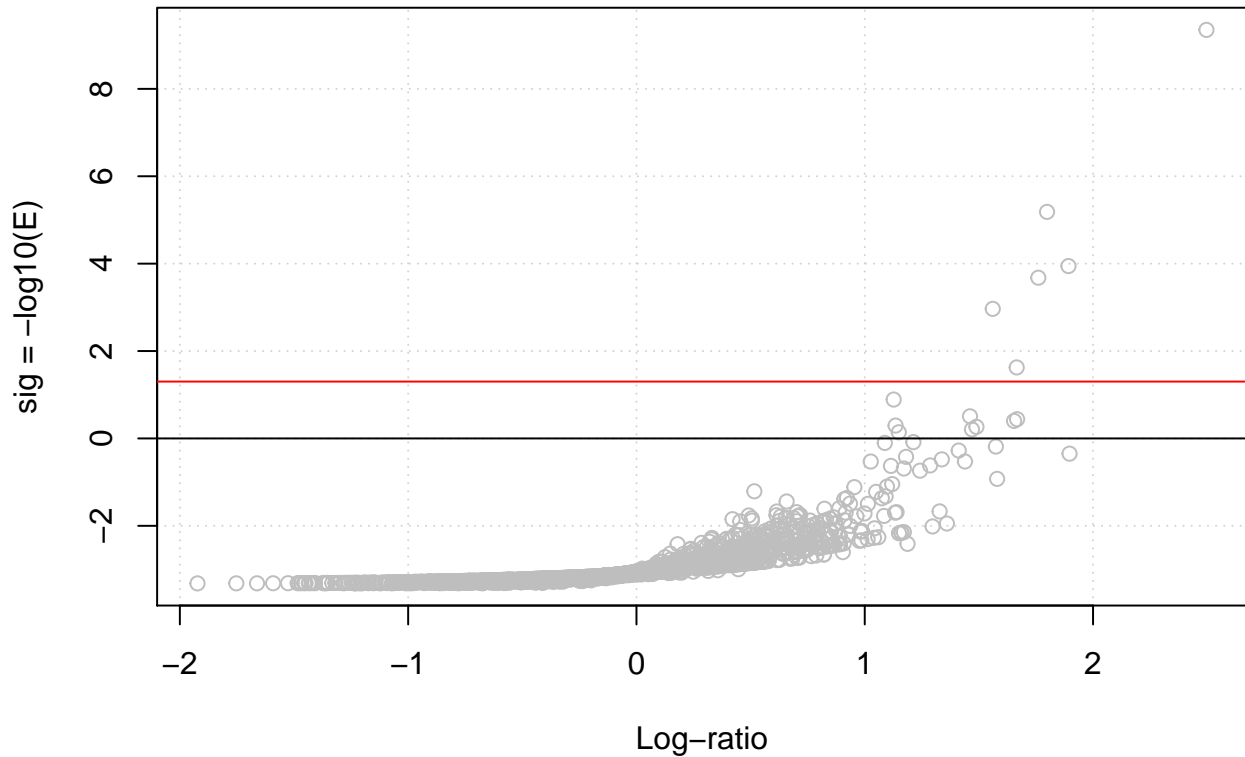
$$sig = -\log_{10}(E)$$

```
oligo.table$eval <- oligo.table$pval * nbTests
oligo.table$sig <- -log10(oligo.table$eval)
```

12. Draw a **Volcano plot**, with the significance as a function of the log-ratio.

```
plot(oligo.table$lr, oligo.table$sig,
     col = "grey",
     xlab = "Log-ratio",
     ylab = "sig = -log10(E)",
     panel.first = grid())
abline(h = 0)

alpha <- 0.05
abline(h = -log10(alpha), col = "red")
```



13. Compute the P-value using the Poisson distribution as approximation of the binomial. Are we in suitable conditions for this approximation? Draw a plot comparing the P-values obtained by the binomial and Poisson distributions.

```
lambda <- oligo.table$exp_occ * sum(oligo.table$occ) / sum(oligo.table$exp_occ)

oligo.table$pval_Poisson <- ppois(
  q = oligo.table$occ - 1, lambda = lambda, lower.tail = FALSE)

plot(oligo.table$pval, oligo.table$pval_Poisson,
     log = "xy")
abline(a = 0, b = 1)
```

